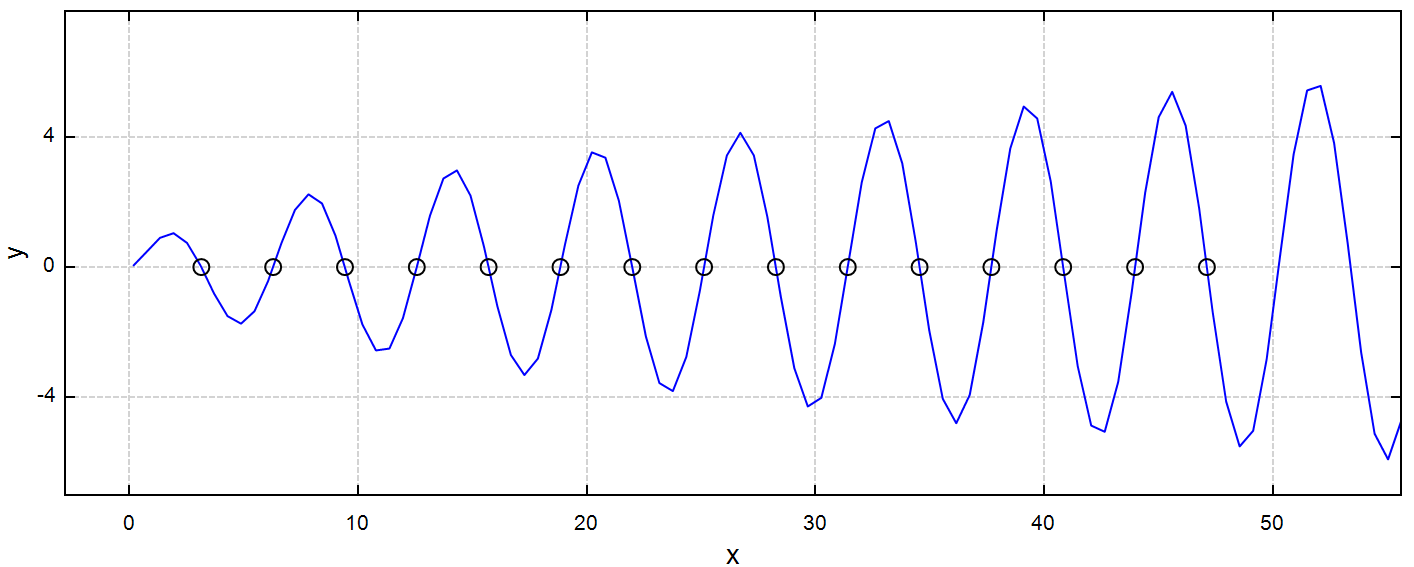


$$F(\mu) := \mu \cdot \sqrt{\frac{2}{\pi \cdot \mu}} \cdot \sin(\mu) - 0.008 \cdot \sqrt{\frac{2}{\pi \cdot \mu}} \cdot \cos(\mu)$$

$$\overrightarrow{\text{check}(\mu)} := -\text{trunc}(\log_{10}(|F(\mu)|)) \quad (\text{Bigger is better})$$

$$\mu_n := \text{solve}(F(\mu) = 0, \mu, 0, 50) = \begin{bmatrix} 3.14413652563747 \\ 6.28445825887869 \\ 9.42562670216452 \\ 12.5670072011288 \\ 15.7084725466544 \\ 18.849980325127 \\ 21.9915123518179 \\ 25.1330595345618 \\ 28.2746164218472 \\ 31.4161811817262 \\ 34.5577503834108 \\ 37.6993240484474 \\ 40.8409004068643 \\ 43.9824790408622 \\ 47.1240595682305 \end{bmatrix} \quad \text{check}(\mu_n) = \begin{bmatrix} 6 \\ 7 \\ 7 \\ 8 \\ 8 \\ 10 \\ 10 \\ 11 \\ 5 \\ 10 \\ 5 \\ 9 \\ 6 \\ 10 \\ 8 \end{bmatrix}$$



$$\begin{cases} F(\mu) \\ \text{augment}(\mu_n, \overrightarrow{\text{check}(\mu_n)}, "o") \end{cases}$$

First you can check the solvers in the NonLinearSolvers plugin. You can read about them in the Martin Kraska handbook in the Plugin / Interactive books plugin or here [https://en.smath.com/forum/yaf\\_postst1508p4\\_NonlinearSolvers-plugin.aspx](https://en.smath.com/forum/yaf_postst1508p4_NonlinearSolvers-plugin.aspx)

Second, you can try `al_nleqsolve`, which is the most powerful pure numerical solver available for now in SMath.

Third, you can write your own routines

$$\text{feval}(\#fs\#, \#x\#) := \text{str2num}(\text{concat}(\text{num2str}(\#fs\#), "(", \text{num2str}(\#x\#), ")"))$$

$$\text{Bis}(f\#, a0\#, b0\#, \varepsilon y\#, \varepsilon x\#) := \begin{bmatrix} a\# & b\# \\ \text{feval}(f\#, a\#) & \text{feval}(f\#, b\#) \end{bmatrix}$$

```

[ya# yb#] := [ feval ( f# , a# ) feval ( f# , b# ) ]
if sign(ya#) = sign(yb#)
  error("Bad interval")
else if |ya#| ≤ εy# · UnitsOf(ya#)
  c# := a#
else if |yb#| ≤ εy# · UnitsOf(yb#)
  c# := b#
else
  N# := 1 + round (  $\frac{\ln \left( \left| \frac{b\# - a\#}{\text{UnitsOf}(b\# - a\#)} \right| \right) - \ln(\epsilon x\#)}{\ln(2)}$  , 0 )
  for iter# ∈ [1..N#]
    [ c# := eval ( 0.5 · ( a# + b# ) ) yc# := feval ( f# , c# ) ]
    if |yc#| ≤ εy# · UnitsOf(yc#)
      break
    else
      if sign(yb#) · sign(yc#) > 0
        [ b# yb# ] := [ c# yc# ]
      else
        [ a# ya# ] := [ c# yc# ]
  c#

```

```

NR1 ( f# , a# , εy# , εx# , δx# , MI# ) := t# := a#
for iter# ∈ [1..MI#]
  [ x# := t# y# := feval ( f# , x# ) ]
  if |y#| ≤ εy# · UnitsOf(y#)
    break
  else
    t# := eval (  $x\# - \frac{\delta x\# \cdot \text{UnitsOf}(x\#) \cdot y\#}{\text{feval}(f\#, x\# + \delta x\# \cdot \text{UnitsOf}(x\#)) - y\#}$  )
    if |x# - t#| < εx# · UnitsOf(x# - t#)
      break
  if iter# = MI#
    error("MaxIters rached.")
  else
    t#

```

Usual values      εy := 0

εx := 10<sup>-15</sup>      δx := 10<sup>-12</sup>

k := [ 1 .. length ( μn ) ]

use the results of solve as interval for Bis or guess values for NR

$\mu b_k := \text{Bis} ( F , \mu n_k - 0.5 , \mu n_k + 0.5 , \epsilon y , \epsilon x ) =$	<table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>3.14413706643403</td></tr> <tr><td>6.28445828812908</td></tr> <tr><td>9.42562671049443</td></tr> <tr><td>12.5670072017972</td></tr> <tr><td>15.7084725472111</td></tr> <tr><td>18.8499803251392</td></tr> <tr><td>21.991512351822</td></tr> <tr><td>25.1330595345624</td></tr> <tr><td>28.2746168215903</td></tr> <tr><td>31.4161811817374</td></tr> <tr><td>34.5577506860319</td></tr> <tr><td>37.6993240484707</td></tr> <tr><td>40.8409003787322</td></tr> <tr><td>43.9824790408665</td></tr> <tr><td>47.1240595685063</td></tr> </table>	3.14413706643403	6.28445828812908	9.42562671049443	12.5670072017972	15.7084725472111	18.8499803251392	21.991512351822	25.1330595345624	28.2746168215903	31.4161811817374	34.5577506860319	37.6993240484707	40.8409003787322	43.9824790408665	47.1240595685063	<table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>14</td></tr> <tr><td>13</td></tr> <tr><td>14</td></tr> <tr><td>12</td></tr> <tr><td>13</td></tr> <tr><td>12</td></tr> <tr><td>13</td></tr> <tr><td>12</td></tr> <tr><td>13</td></tr> <tr><td>12</td></tr> <tr><td>12</td></tr> <tr><td>13</td></tr> <tr><td>12</td></tr> <tr><td>12</td></tr> <tr><td>13</td></tr> <tr><td>12</td></tr> <tr><td>12</td></tr> </table>	14	13	14	12	13	12	13	12	13	12	12	13	12	12	13	12	12
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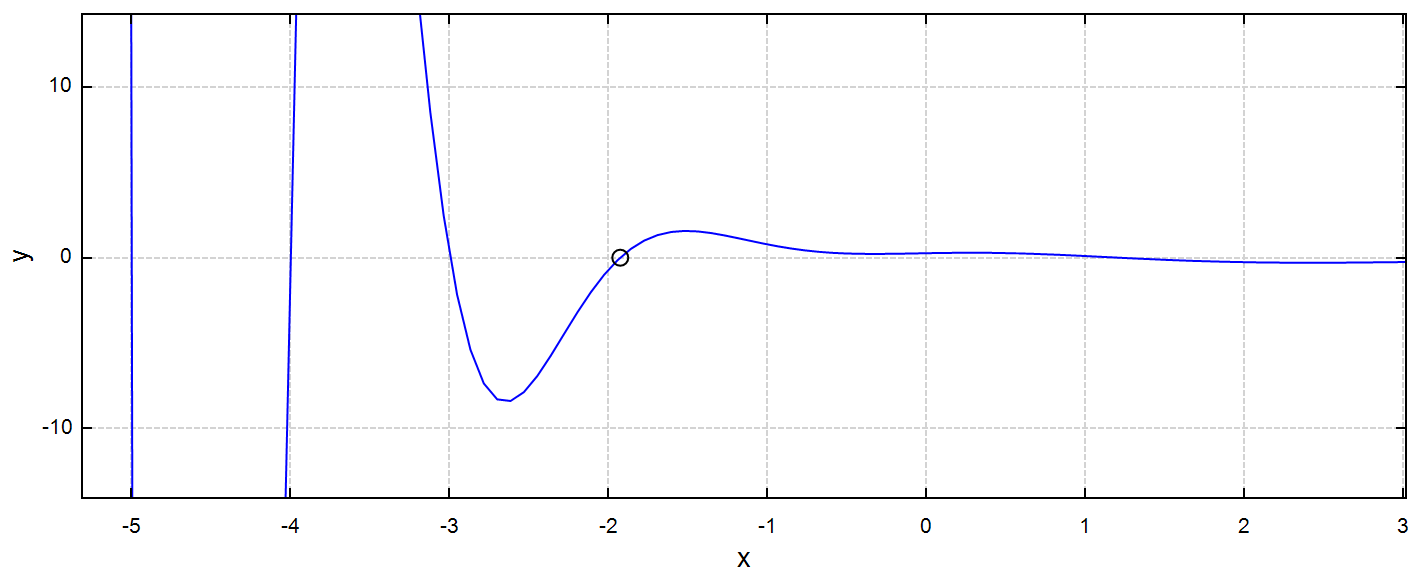
$$\mu r_k := NR_1(F, \mu n_k, \varepsilon y, \varepsilon x, \delta x, 10) = \begin{bmatrix} 3.14413706643404 \\ 6.28445828812909 \\ 9.42562671049443 \\ 12.5670072017973 \\ 15.7084725472111 \\ 18.8499803251393 \\ 21.991512351822 \\ 25.1330595345624 \\ 28.2746168215903 \\ 31.4161811817373 \\ 34.5577506860319 \\ 37.6993240484706 \\ 40.8409003787322 \\ 43.9824790408664 \\ 47.1240595685063 \end{bmatrix} \quad \text{check}(\mu r) = \begin{bmatrix} 14 \\ 14 \\ 14 \\ 13 \\ 13 \\ 13 \\ 13 \\ 12 \\ 13 \\ 13 \\ 12 \\ 12 \\ 13 \\ 13 \\ 12 \end{bmatrix}$$

solve, and the solvers in NonLinearSolvers can't work with functions defined in plugins, like Bessel ones.

$$Y(v) := v \cdot \text{BesselJ}(v, 1) - 1.01 \cdot \text{BesselJ}(v, 3)$$

$$v_0 := \text{Bis}(Y, -2.5, -1, 0, \varepsilon x) = -1.92464715696971$$

$$v_0 := NR_1(Y, -2, \varepsilon y, \varepsilon x, \delta x, 10) = -1.9246471569697$$



$$\left\{ \begin{array}{l} Y(v) \\ \text{augment}(v_0, Y(v_0), "o") \end{array} \right.$$

Alvaro