

Fitting function to data
 - single variable, linear on parameters

$$T := \begin{pmatrix} -36.7 \\ -19.6 \\ -11.5 \\ -2.6 \\ 7.6 \\ 15.4 \\ 26.1 \\ 42.2 \\ 60.6 \\ 80.1 \end{pmatrix} \quad p := \begin{pmatrix} 1 \\ 5 \\ 10 \\ 20 \\ 40 \\ 60 \\ 100 \\ 200 \\ 400 \\ 760 \end{pmatrix} \quad T := T + 273$$

```
for i ∈ 1..length(p)
    y_i := log10(p_i)
```

$$T = \begin{pmatrix} 236.3 \\ 253.4 \\ 261.5 \\ 270.4 \\ 280.6 \\ 288.4 \\ 299.1 \\ 315.2 \\ 333.6 \\ 353.1 \end{pmatrix} \quad y = \begin{pmatrix} 0 \\ 0.699 \\ 1 \\ 1.301 \\ 1.6021 \\ 1.7782 \\ 2 \\ 2.301 \\ 2.6021 \\ 2.8808 \end{pmatrix}$$

//The expression we are interested in
 //T-independent variable, b-vector of unknown parameters

$$\log_{10}(p) = b_1 + \frac{b_2}{T} + b_3 \cdot \log_{10}(T) + b_4 \cdot T^2$$

//from the function above we construct a vector function

$$\varphi(x) := \begin{pmatrix} 1 \\ \frac{1}{x} \\ \log_{10}(x) \\ x^2 \end{pmatrix}$$

```
n := length(T)    k := length(phi(x))
```

```
n = 10           k = 4
```

//X-matrix, matrix of experiment

```
for j ∈ 1..k
    for i ∈ 1..n
        X_ij := phi(T_i)_j
```

```
Phi := X^T * X    d := X^T * y
```

```
b := eval(phi^-1).d
```

$$b = \begin{pmatrix} 216.2057 \\ -9295.4875 \\ -75.5676 \\ 4.4384 \cdot 10^{-5} \end{pmatrix} \quad \begin{array}{l} //Unknown parameters \\ //found in the least-square sense \end{array}$$

```
pcalc(x):=eval(10b·φ(x))
```

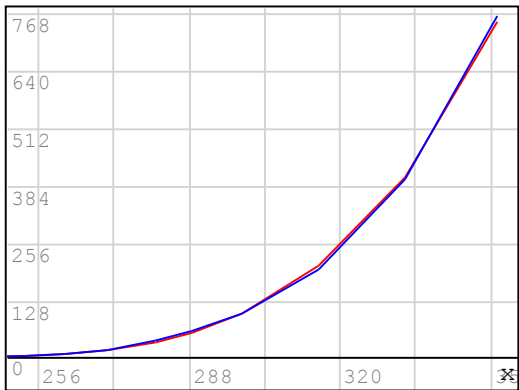
```
for i∈1..length(T)
```

```
pci:=pcalc(Ti)
```

Calculated

Given

pc=	$\begin{pmatrix} 0.9757 \\ 5.2798 \\ 10.2648 \\ 19.6372 \\ 37.7525 \\ 58.8916 \\ 101.516 \\ 205.2468 \\ 404.3377 \\ 750.7548 \end{pmatrix}$	p=	$\begin{pmatrix} 1 \\ 5 \\ 10 \\ 20 \\ 40 \\ 60 \\ 100 \\ 200 \\ 400 \\ 760 \end{pmatrix}$



Data
Fit

```
{ augment(T, p)  
  augment(T, pc)
```

```
//The standard error of function:
```

$$s := \sqrt{\frac{1}{n-k} \cdot (p - pc)^2} \quad s = 4.8421$$

```
//END
```